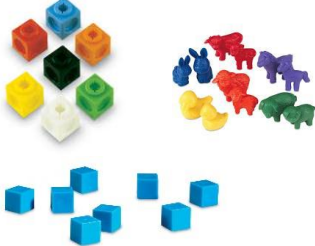




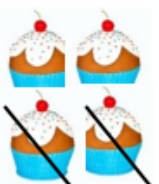
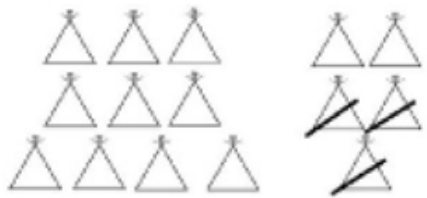

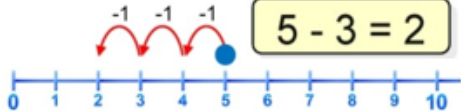

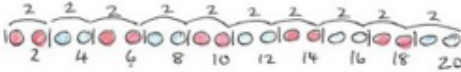
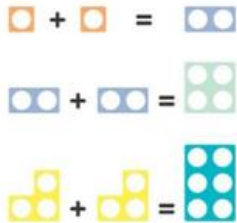

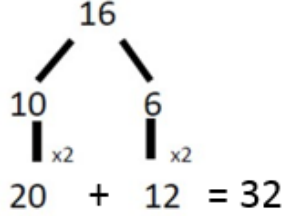
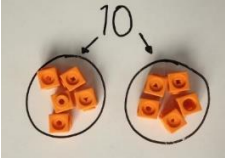
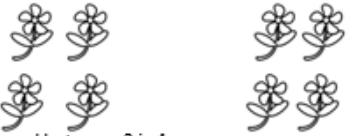

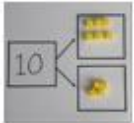

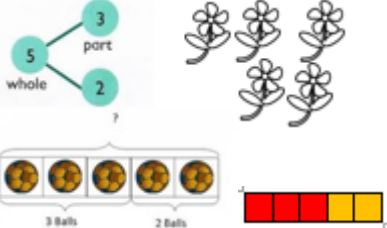
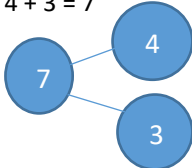
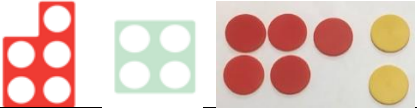
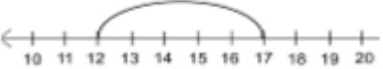
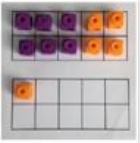

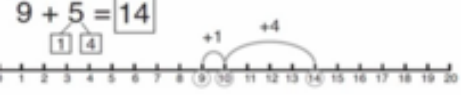

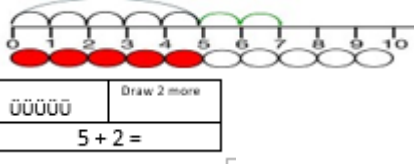



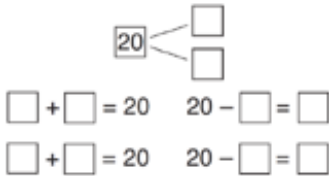
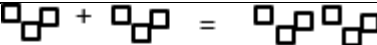
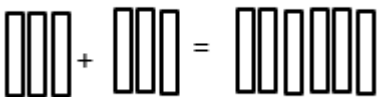



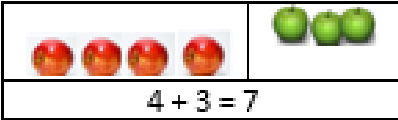
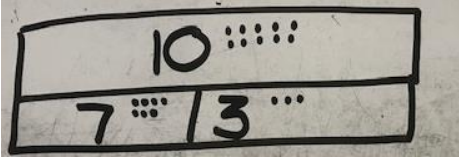
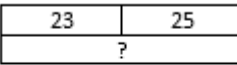
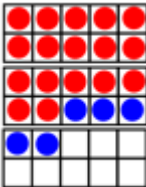
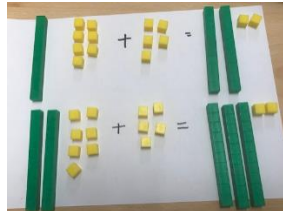
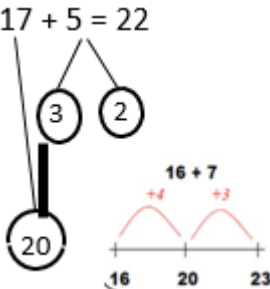


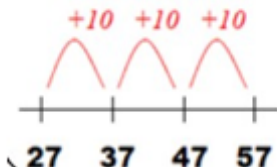

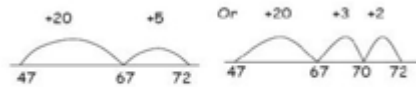




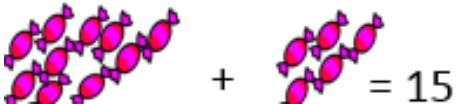
Early Learning Goal	Concrete	Pictorial	Abstract	YR
Count reliably with numbers from 1 to 20	Use a variety of objects to count different groups of 1 to 20 	Use pictures to count groups	Count groups using numbers and counting aloud. Subsidising numbers on dice for board games	<div data-bbox="1915 156 2018 228">YR</div> <div data-bbox="2011 411 2101 1294">Early Years Calculation</div>
Add two single-digit numbers	Use cubes to add 2 numbers together as a group.  Using the part-whole model. 	Use pictures to add 2 single digit numbers 	Use abstract knowledge to add 2 single digit numbers. $3 + 2 = 5$	
Subtract two single-digit numbers	Use physical objects, counters, cubes to show how objects can be taken away.  $6 - 4 = 2$  $4 - 2 = 2$	Cross out drawn objects to show what has been taken away.  $15 - 3 = 12$	$7 - 4 = 3$ $16 - 9 = 7$	

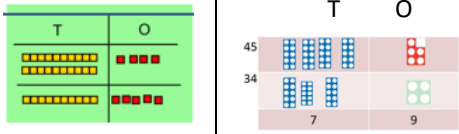
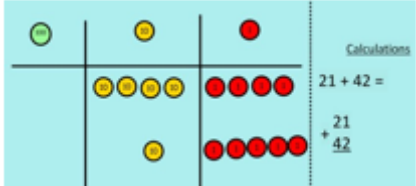

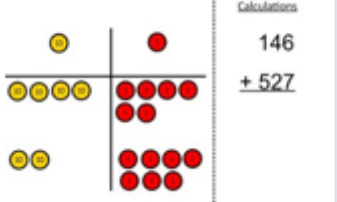
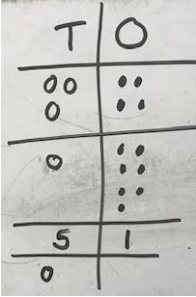
Early Learning Goal	Concrete	Pictorial	Abstract	YR
Counting forwards and backwards	<p>Move objects towards and away from the group.</p> 	<p>Count back in ones using a number line.</p> 	<p>Put 13 in your head, count back 4. What number are you at?</p>	<h1>Early Years Calculation</h1>
Counting in steps of 2	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>Children make representations to show counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>	
Doubling numbers to 10	<p>Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling.</p> 	<p>Draw pictures to show how to double numbers.</p> <p>Double 4 is 8</p> 	<p>Partition a number and then double each part before recombining it back together.</p> 	
Halving even numbers less than 20	<p>Sharing numbers into 2 groups I have 10 cubes, can you share them equally in 2 groups?</p> 	<p>Children draw a picture to show the sharing</p>  <p>8 shared between 2 is 4</p>	<p>12 shared between 2 is 6</p>	

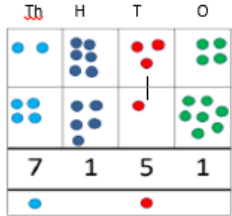
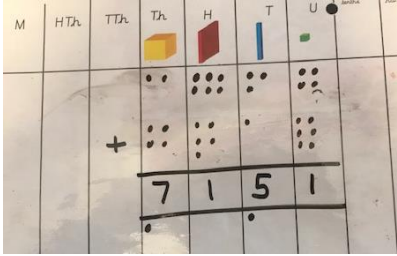
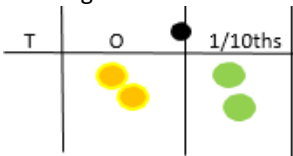
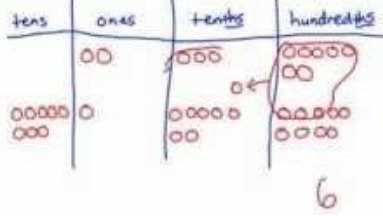
Objective and Strategy	Concrete	Pictorial	Abstract	<div data-bbox="1921 156 2027 228">Y1</div> <div data-bbox="1899 411 2063 1169">Addition</div>
Combining two parts to make a whole: part-whole model	Use cubes and other counting objects to add 2 numbers together as a group.  Using the part-whole model.   And bar model.	Use pictures to add 2 numbers together as a group or a bar. 	$4 + 3 = 7$  Use the part-whole diagram or the abstract: $7 = 4 + 3$	
Starting at the bigger number and counting on	Start with the larger number then count on the smaller number 1 by 1 to find the answer. 	Use a number line and jump in ones from the larger number. $12 + 5 = 17$ 	$5 + 12 = 17$ Place the larger number in your head and count on the smaller number to find the answer.	
Regrouping to make 10. <i>This is an essential skill for column addition later.</i>	e.g. $6 + 5 =$ Start with the bigger number and use the smaller number to make 10. Use ten frames. 	 $3 + 9 =$ Use pictures or a number line. Regroup or partition the smaller number using the part-whole model to make 10. $9 + 5 = 14$ 	$7 + 4 = 11$ If I am at 7, how many more do I need to make 10? How many more do I need to add on now?	
Represent & use number bonds and related subtraction facts within 20	 2 more than 5	 $5 + 2 =$	Emphasis should be on the language: '1 more than 5 is equal to 6.' '2 more than 5 is 7.' Introduce the > and < signs	

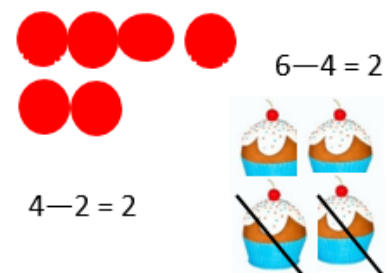
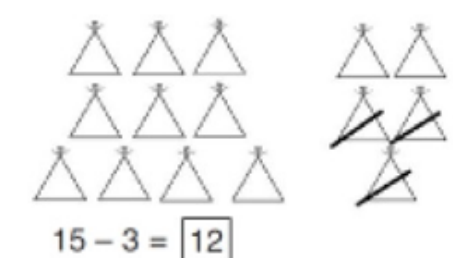

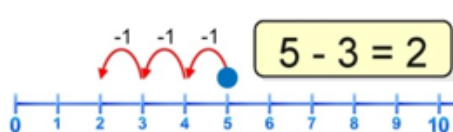
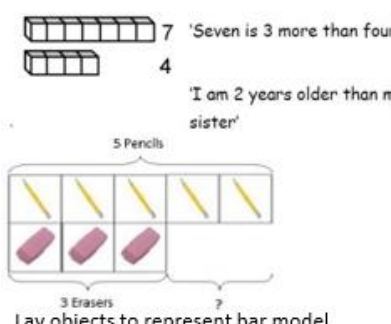

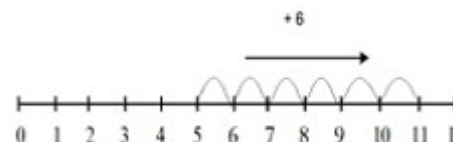
Objective and Strategy	Concrete	Pictorial	Abstract	Y2
Adding multiples of 10	$50 = 30 + 10$  Use dienes or bead strings	Use representations for base ten  $3 \text{ tens} + 5 \text{ tens} = \underline{\hspace{2cm}} \text{ tens}$ $30 + 50 = \underline{\hspace{2cm}}$	$20 + 30 = 50$ $70 = 50 + 20$ $40 + \square = 60$	
Use known number facts Part-whole	Children explore different ways of making numbers within 20. 		$\square + 1 = 16$ $1 + \square = 16$ $16 - 1 = \square$ $16 - \square = 1$	Addition
Using known facts	 	   Children draw representations of H, T, O	$3 + 4 = 7$ leads to $30 + 40 = 70$ leads to $300 + 400 = 700$	
Bar model	 $4 + 3 = 7$	 $7 + 3 = 10$	 $23 + 25 = 48$	

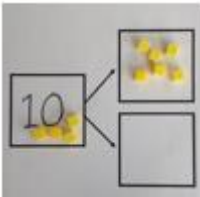
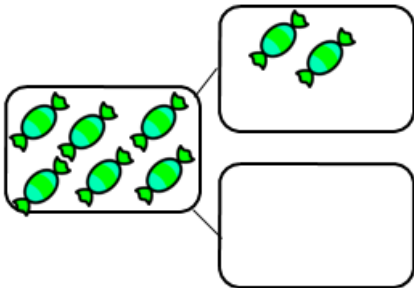
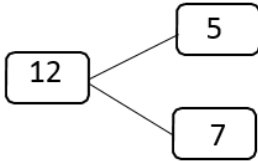


Objective and Strategy	Concrete	Pictorial	Abstract	Y2			
Add a two digit number and ones	<p>$17 + 5 = 22$</p>  <p>Use ten frame to make 'magic ten'</p> <p>Children explore the patterns</p> <p>$17 + 5 = 22$</p> <p>$27 + 5 = 32$</p> 	<p>Use part-whole model and number lines</p> <p>$17 + 5 = 22$</p> 	<p>$17 + 5 = 22$</p> <table border="1" data-bbox="1442 397 1688 461"><tr><td>17</td><td>5</td></tr><tr><td colspan="2">22</td></tr></table> <p>Make explicit the related facts</p> <p>$17 + 5 = 22$</p> <p>$5 + 17 = 22$</p> <p>$22 - 5 = 17$</p> <p>$22 - 17 = 5$</p>		17	5	22
17	5						
22							
Add a 2 digit number and tens	<p>$25 + 10 = 35$</p>   <p>Explore that the ones digit does not change, 100 square to investigate number sense.</p>	<p>$27 + 30$</p> 	<p>$27 + 10 = 37$</p> <p>$27 + 20 = 47$</p> <p>$27 + \square = 57$</p>	Addition			
Add 2 two-digit numbers	 <p>Model using dienes, place value counters and numicon</p>	 <p>Use number line and bridge ten using part whole if necessary.</p>	<p>$25 + 47$</p> <p>Only partition 1 number</p> <p>$(47 = 40 + 7)$</p> <p>$25 + 40 = 65$</p> <p>$65 + 7 = 72$</p>				

<p>Add three 1-digit numbers</p>	 <p>Combine to make 10 first if possible, or bridge 10 then add third digit. Use dienes, place value counters, ten frames and numicon</p>	 <p>Regroup and draw representation.</p> 	<p>Combine 2 numbers that make or bridge 10, then add third number.</p> $4 + 7 + 6 =$ $4 + 6 = 10$ $10 + 7 = 17$	
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Objective and Strategy	Concrete	Pictorial	Abstract	Y3 Addition
Column Addition—no regrouping (friendly numbers)	<p>Model using Dienes & numicon. Add the ones first, then the tens.</p>  <p>Moving to place value counters.</p> 	<p>Children move to drawing the counters using a tens and one frame.</p> 	<p>Add the ones first, then the tens, then the hundreds.</p> $\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 200 + 20 + 3 \\ 100 + 10 + 4 \\ \hline 300 + 30 + 7 = 337 \end{array}$	
Column Addition with regrouping.	<p>Exchange ten ones for a ten, using PV counters.</p> 	<p>Children can draw a representation of the grid to further support their understanding, carrying the ten <u>underneath</u> the line.</p> 	<p>Start by partitioning the numbers.</p> $\begin{array}{r} \text{T} \quad \text{O} \\ 20 + 5 \\ 40 + 8 \\ \hline 60 + 13 = 73 \end{array}$ <p>Then use the formal column to show the exchange.</p> $\begin{array}{r} \text{T} \quad \text{O} \\ 2 \quad 5 \\ + 4 \quad 8 \\ \hline 7 \quad 3 \\ \hline 1 \end{array}$	

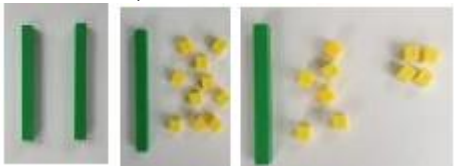
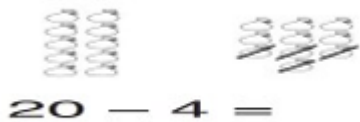
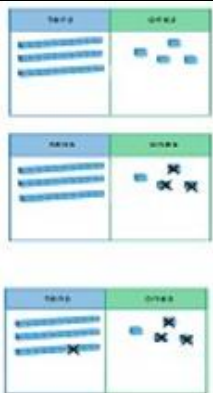

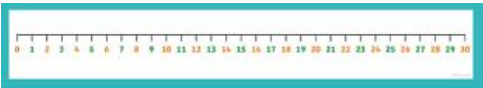
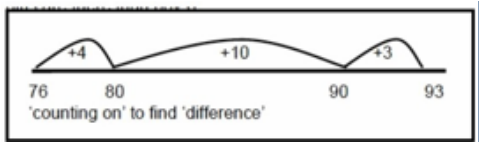
Objective and Strategy	Concrete	Pictorial	Abstract	<div>Y4-6</div> <div>Addition</div>
<p>Year 4</p> <p>Add numbers with up to 4 digits</p>	<p>Children continue to use PV counters to add and understand the concept of exchanging between the PV columns.</p> 	<p>Draw representations using PV grid.</p> 	<p>Continue from previous work to include carrying hundreds.</p> <p>Relate to money and measures.</p> <p>Th H T O</p> $\begin{array}{r} 3517 \\ + 396 \\ \hline 3913 \end{array}$	
<p>Year 5</p> <p>Add numbers with more than 4 digits.</p> <p>Add decimals with 2 decimal places, including money.</p>	<p>Continue to use PV Counters and introduce decimal place value counters to model exchange.</p> 	<p>$2.37 + 81.79$</p> 	<p>T O . 1/10^{ths} 1/100^{ths}</p> $\begin{array}{r} £23.59 \\ + £7.55 \\ \hline £31.14 \end{array}$	
<p>Year 6</p> <p>Add several numbers of increasing complexity.</p> <p>Important to be in the context of money and measure using 3dp</p>	<p>See above</p>	<p>See above</p>	<p>Insert place holders!</p> $\begin{array}{r} 23.361 \\ 9.080 \\ 59.770 \\ + 1.300 \\ \hline 93.511 \end{array}$	

Objective and Strategy	Concrete	Pictorial	Abstract	Y1 Subtraction			
Taking away ones.	<p>Use physical objects, counters, cubes to show how objects can be taken away.</p> 	<p>Cross out drawn objects to show what has been taken away.</p> 	<p>$7 - 4 = 3$</p> <p>$16 - 9 = 7$</p>				
Counting back	<p>Move objects away from the group.</p> 	<p>Count back in ones using a number line.</p> 	<p>Put 13 in your head, count back 4. What number are you at?</p>				
Find the difference	<p>Compare objects and amounts.</p>  <p>Lay objects to represent bar model.</p> <p>Use two-sided counters</p> 	<p>Count on using a number line to find the difference.</p>  <p>Difference between 5 and 11</p> <table border="1" data-bbox="913 1265 1077 1343"><tr><td colspan="2">11</td></tr><tr><td>5</td><td>?</td></tr></table>	11		5	?	<p>Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?</p>
11							
5	?						

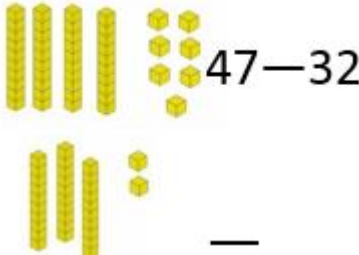
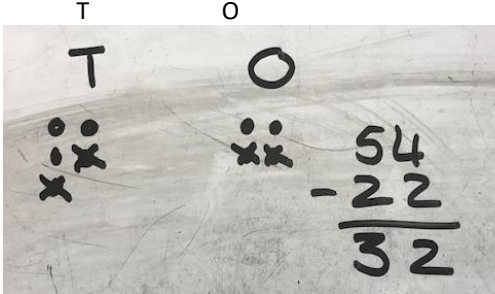
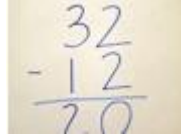

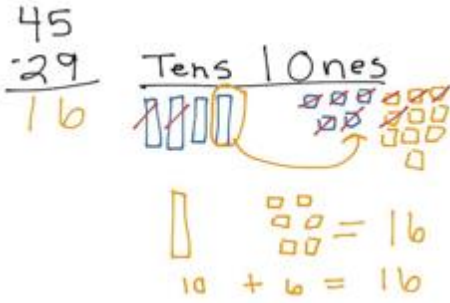
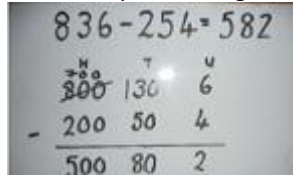
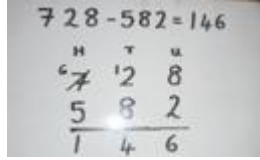
Objective and Strategy	Concrete	Pictorial	Abstract	Y1			
Represent and use number bonds and related subtraction facts within 20	<p>Link to addition. Use Part-whole model to link to the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what s the other part? 10-6 =?</p> 	<p>Use pictorial representations to show the part-whole.</p> 	<p>Move to using numbers</p> 	<h1>Subtraction</h1>			
	<p>Bar Model</p>  <p>$5 - 2 = 3$</p>		<table border="1"><tr><td colspan="2">10</td></tr><tr><td>8</td><td>2</td></tr></table> <p>$10 = 8 + 2$ $10 = 2 + 8$ $10 - 2 = 8$ $10 - 8 = 2$</p>		10		8
10							
8	2						

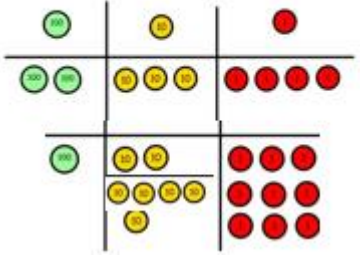
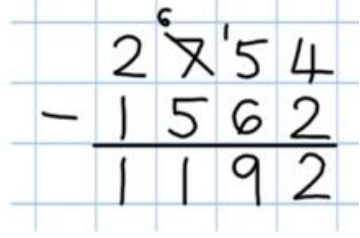
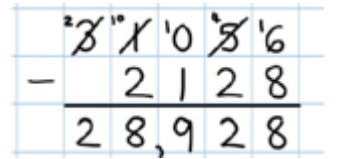
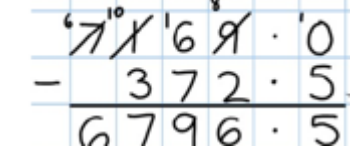
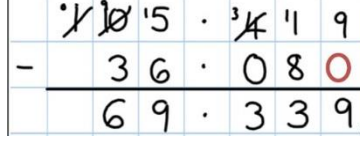
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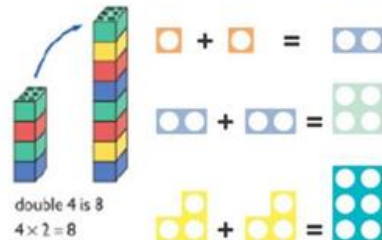

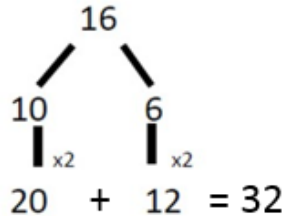
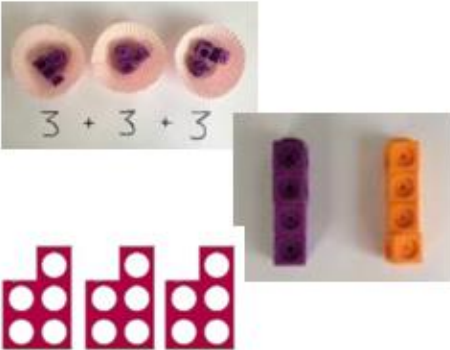
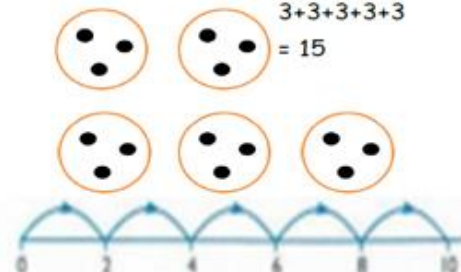

subtraction

Objective and Strategy	Concrete	Pictorial	Abstract	
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make' 	 $20 - 4 =$	Use what we know to help calculate, e.g. number bonds, $20 = 10 + 10$, number bond for 10 and 4 is? $20 - 4 = 16$	
Partitioning to subtract without regrouping. <i>'Friendly numbers'</i>	$34 - 13 = 21$ Use Dienes to show how to partition the number when subtracting without regrouping. 	Draw a representation so can cross off.  $43 - 21 = 22$	$43 - 21 = 22$	
Make ten strategy <i>Progression should be crossing one ten, crossing more than one ten, cross- ing the hundreds.</i>	Use a number line to model counting to next ten and the rest. $24 - 16$ 	Use a number line to count on to next ten and then the rest. 	$93 - 76 = 17$ $28 + \square = 34$	

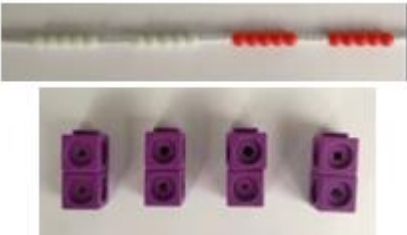
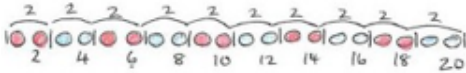
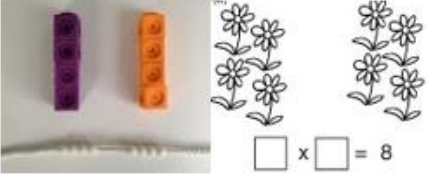

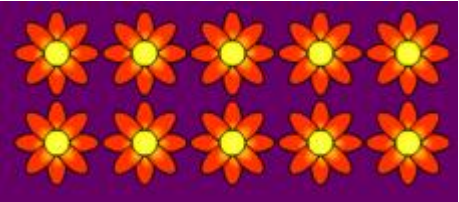
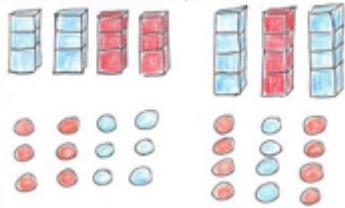
				
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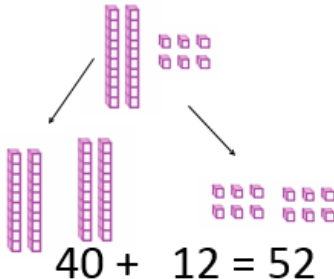
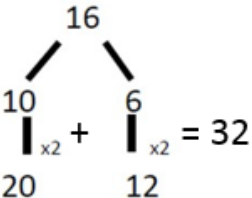
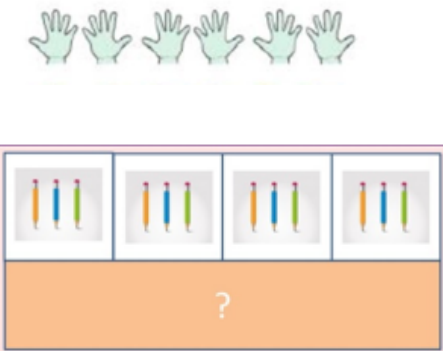
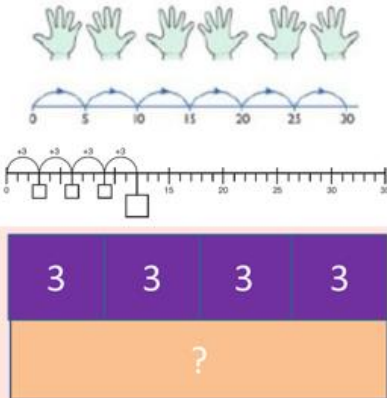
Objective and Strategy	Concrete	Pictorial	Abstract	Y3
Column subtraction without regrouping (friendly numbers)	Use Diennes or Numiocon to model  $47 - 32$	Draw representations to support understanding. 	Intermediate step may be needed to lead to clear subtraction understanding. $47 - 24 = 23$ $\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$ This: 	Subtraction
Column subtraction with regrouping	Begin with Diennes or Numicon. Move to PV counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange. $45 - 29$ 	Children may draw Diennes or PV counters and cross off. $\begin{array}{r} 45 \\ - 29 \\ \hline 16 \end{array}$ 	Start with partitioning $836 - 254 = 582$  To formal method $728 - 582 = 146$ 	

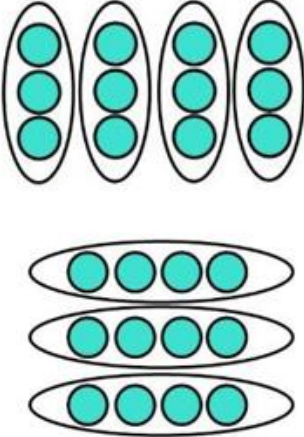

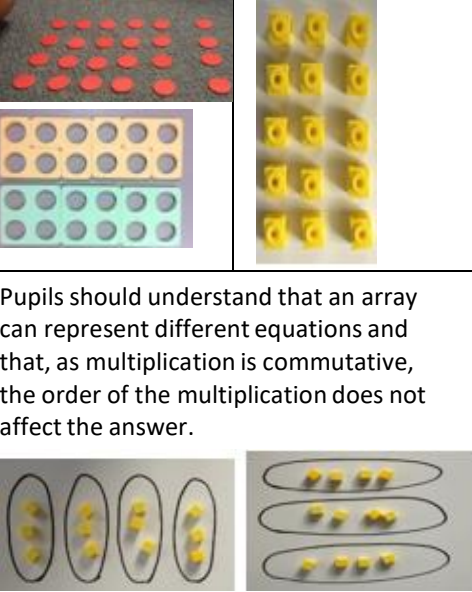

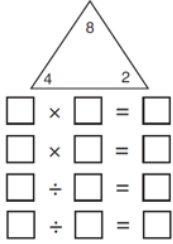
Objective and Strategy	Concrete	Pictorial	Abstract	Y4-6
<p>Subtracting tens and ones</p> <p><u>Year 4</u> - subtract with up-to 4 digits.</p> <p><i>Introduce decimal subtraction through context of money</i></p>	<p>Model exchange using Dienes or PV counters.</p> <p>234 - 179</p> 	<p>Children to draw PV counters and show their exchange (see Year 3)</p>	<p>Use the phrase 'take and make' for exchange.</p> <p>Th H T O</p> 	<h1>Subtraction</h1>
<p><u>Year 5</u> - Subtract with at least 4 digits, including money and measures.</p> <p><i>Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal.</i></p>		<p>Children to draw PV counters and show their exchange (see Year 3)</p>	<p>TTh Th H T O</p>  <p>Remember to use PV holders!</p> <p>Th H T O . 1/10ths</p> 	
<p><u>Year 6</u> - Subtract with increasingly large and more complex numbers and decimal values.</p>				

Objective and Strategy	Concrete	Pictorial	Abstract	Y1
Doubling	<p>Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling.</p> 	<p>Draw pictures to show how to double numbers.</p> <p>Double 4 is 8</p> 	<p>Partition a number and then double each part before recombining it back together.</p> 	<h1 data-bbox="1982 351 2094 1093">multiplication</h1>
Repeated addition	<p>Use different objects to add equal groups.</p> 	<p>Use pictorial including number lines to solve problems.</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>  <p>$3+3+3+3+3 = 15$</p>	<p>Write addition sentences to describe objects and pictures.</p>  <p>$2 + 2 + 2 + 2 + 2 = 10$</p>	

Y1 multiplication

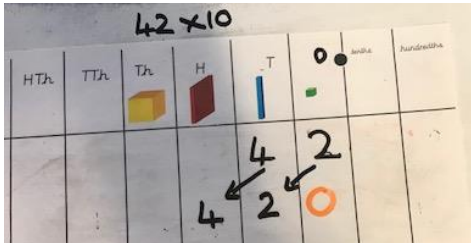
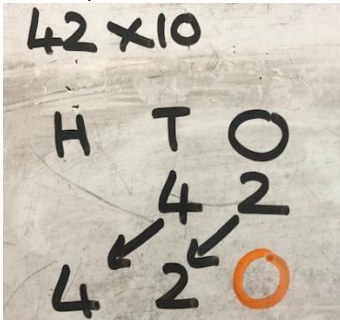
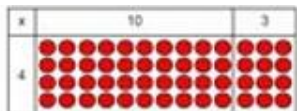
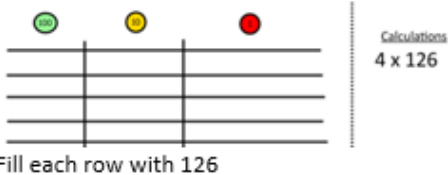
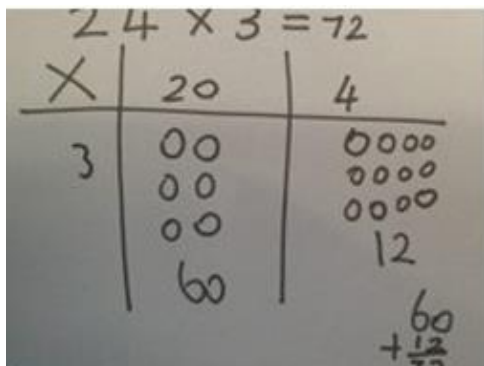
Counting in multiples	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>Children make representations to show counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>	
Making equal groups and counting the total	<p>Use manipulatives to create equal groups or 'lots of'.</p> 	<p>Draw and make representations.</p> <p>Draw  to show $2 \times 3 = 6$</p>	<p>$2 \times 4 = 8$</p>	
Understanding arrays	<p>Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.</p> 	<p>Draw representations of arrays to show understanding.</p> 	<p>$3 \times 2 = 6$</p> <p>$2 \times 5 = 10$</p>	

Objective and Strategy	Concrete	Pictorial	Abstract	Y2
Doubling	<p>Model doubling using Dienes and PV counters.</p>  <p>40 + 12 = 52</p>	<p>Draw pictures and representations to show how to double numbers.</p>	<p>Partition number, then double each part before recombining.</p>  <p>Or near double mental strategy.</p>	multiplication
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models.</p> <p>5 + 5 + 5 + 5 + 5 + 5 = 35</p> 	<p>Number lines, counting sticks and bar models should be used to show representation of counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>0, 2, 4, 6, 8, 10</p> <p>0, 3, 6, 9, 12, 15</p> <p>0, 5, 10, 15, 20, 25, 30</p> <p>4 × 3 = <input type="text"/></p>	

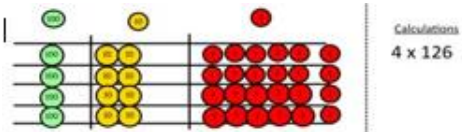
Objective and Strategy	Concrete	Pictorial	Abstract	Y2
<p>Multiplication is commutative</p>	<p>Create arrays using counters and cubes and Numicon.</p>	<p>Use representations of arrays to show different calculations and explore commutativity.</p> 	<p>$12 = 3 \times 4$</p> <p>$12 = 4 \times 3$</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p> $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$ </p>	<p style="writing-mode: vertical-rl; transform: rotate(180deg);">multiplication</p>
	<p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p> 			
<p>Using the Inverse</p> <p><i>This should be taught alongside division, so pupils learn how they work alongside each other.</i></p>			<p> $2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 4 = 2$ $8 \div 2 = 4$ $8 = 2 \times 4$ $8 = 4 \times 2$ $2 = 8 \div 4$ $4 = 8 \div 2$ </p> <p>Show all 8 related fact family sentences.</p>	

Y3

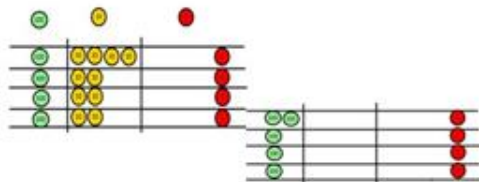
multiplication

Objective and Strategy	Concrete	Pictorial	Abstract	Y3 multiplication															
Multiply a number by 10	Use place value charts to move the digits through the PV columns. 	Draw a place vlaue chart to move the digits. 	Use known facts, $20 \times 3 = 2 \times 3 \times 10$																
Multiply a number by 10 or 100	Use place value charts to move the digits through the PV columns. As above	Draw a place vlaue chart to move the digits. As above	Use known facts, $20 \times 3 = 2 \times 3 \times 10$																
Grid Method	Show the links with arrays to first introduce the grid method.  Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.  Fill each row with 126	Children can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below. 	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. <table border="1" data-bbox="1489 920 1736 994"><tr><td>x</td><td>30</td><td>5</td></tr><tr><td>7</td><td>210</td><td>35</td></tr></table> $210 + 35 = 245$ Moving forward, multiply by a 2 digit number showing the different rows within the grid method. <table border="1" data-bbox="1440 1192 1740 1383"><tr><td></td><td>10</td><td>8</td></tr><tr><td>10</td><td>100</td><td>80</td></tr><tr><td>3</td><td>30</td><td>24</td></tr></table>		x	30	5	7	210	35		10	8	10	100	80	3	30	24
x	30	5																	
7	210	35																	
	10	8																	
10	100	80																	
3	30	24																	

Bar model are used to explore missing number.



Add up each column, starting with the ones making any exchanges needed



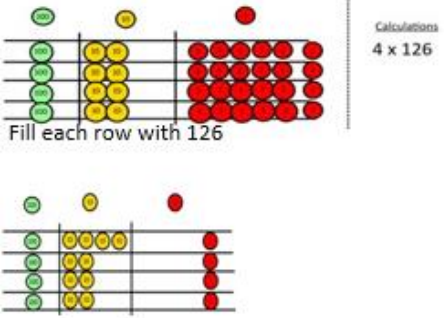
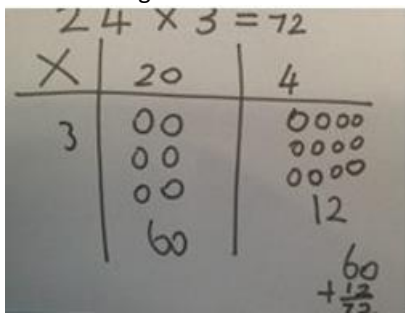
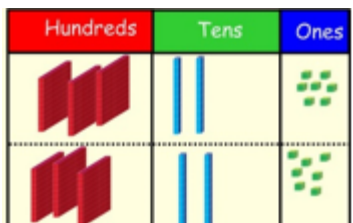
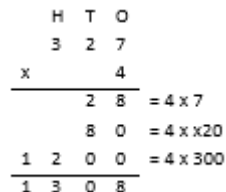
Then you have your answer

$$4 \times \square = 20$$

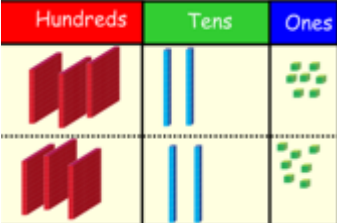
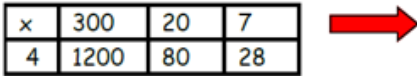
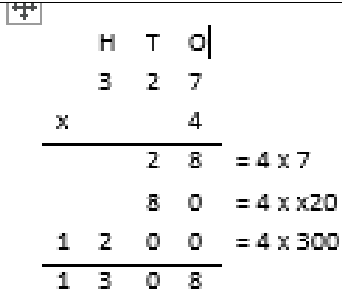

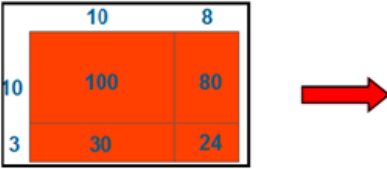
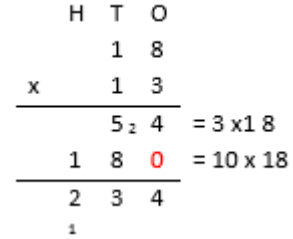
20			
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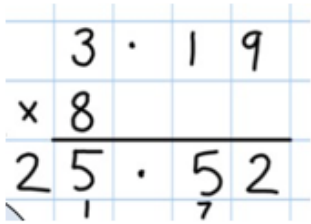
Y4



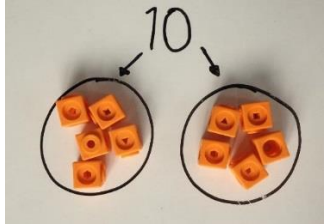
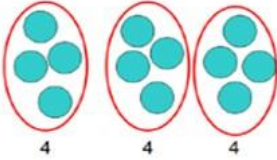
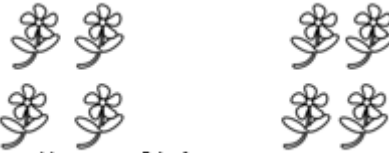
multiplication

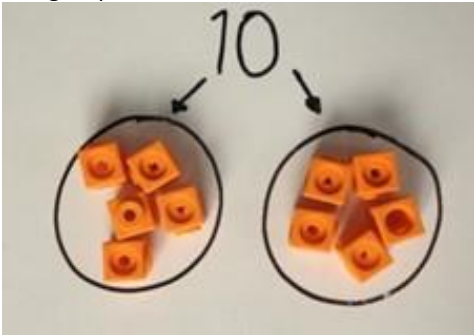
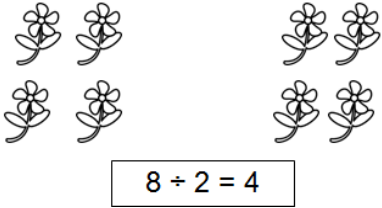
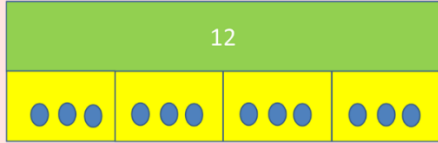
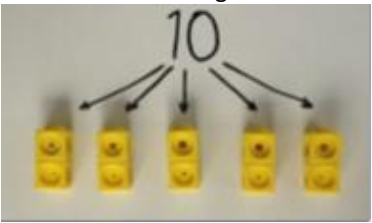
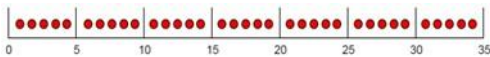
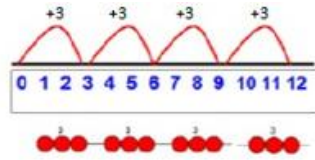
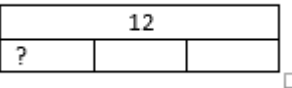
Objective and Strategy	Concrete	Pictorial	Abstract	Y4 multiplication																											
<p>Grid method recap from Year 3 for 2 digits x 1 digit</p> <p>Move to multiplying 3 digit numbers by 1 digit. (Year 4 expectation)</p>	<p>Use place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.</p>  <p>Fill each row with 126</p> <p>Add up each column, starting with the ones and exchange where necessary.</p>	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below</p> 	<p>Start with multiplying by one digit numbers and showing the clear addition alongside the grid.</p> <table border="1"><tr><td>x</td><td>30</td><td>5</td></tr><tr><td>7</td><td>210</td><td>35</td></tr></table> <p>210 + 35 = 245</p>		x	30	5	7	210	35																					
x	30	5																													
7	210	35																													
<p>Column multiplication</p>	<p>Children can continue to be supported by place value counters at this stage of multiplication. This initially done where there is no regrouping. 321 x 2 = 642</p>  <p>Remember to add from the ones!</p>	<p>The grid method may be used to show how this relates to a formal written method.</p> <table border="1"><tr><td>x</td><td>300</td><td>20</td><td>7</td></tr><tr><td>4</td><td>1200</td><td>80</td><td>28</td></tr></table> <p>Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.</p>	x	300	20	7	4	1200	80	28	 <p>Then moving to the contracted method.</p> <table><tr><td></td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td>3</td><td>2</td><td>7</td></tr><tr><td>x</td><td></td><td></td><td>4</td></tr><tr><td></td><td>1</td><td>3</td><td>0</td></tr><tr><td></td><td>1</td><td>2</td><td></td></tr></table>		H	T	O		3	2	7	x			4		1	3	0		1	2	
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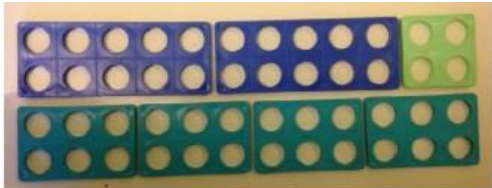


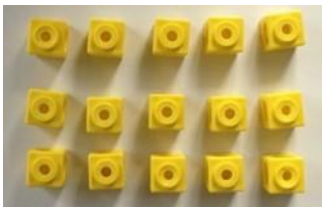
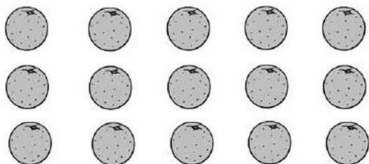
$8 \sim 54$
 $= 8 \times 60 - 8$
 $8 \times 6 = 48$
 $8 \times 60 = 480$
 $480 - 8 = (472)$

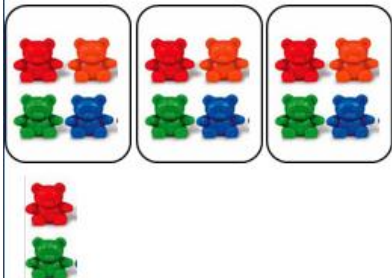
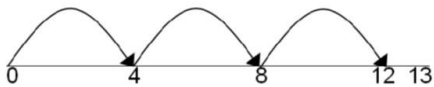

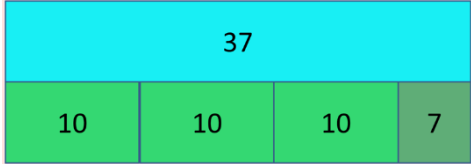
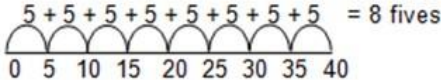
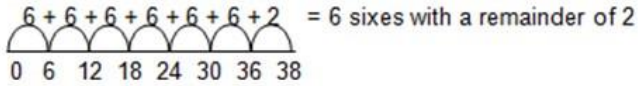

Objective and Strategy	Concrete	Pictorial	Abstract	Y5-6
<p>Column Multiplication for 3 and 4 digits x 1 digit.</p>	<p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$</p> <p>It is important that they always multiply the ones first.</p> 	<p>$327 \times 7 =$</p> 	 <p>Which leads to the contracted method.</p> 	<h1 style="writing-mode: vertical-rl; transform: rotate(180deg);">multiplication</h1>
<p>Column multiplication for x by 2 digit</p>	<p>Manipulatives can be used alongside the written method.</p>	<p>$18 \times 13 =$</p> 	<p>Using the contracted formal method</p>  <p>Remember you place value holder</p>	

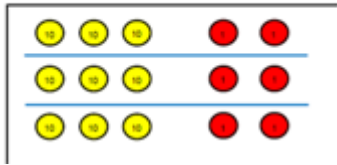


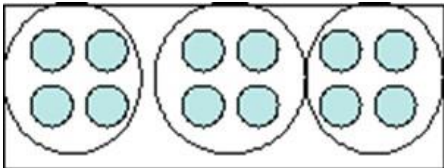
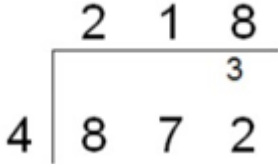
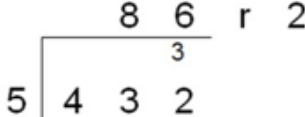
Objective and Strategy	Concrete	Pictorial	Abstract	multiplication
<p>Multiplying decimals up to 2 decimal places by a single digit.</p>			<p>Remind children that the single digit belongs in the ones column. Line up the decimal points in the question and the answer.</p> <p>O . 1/10ths 1/100ths</p> 	

Objective and Strategy	Concrete	Pictorial	Abstract	Y1
Division as sharing, groups of, lots of	<div data-bbox="486 284 813 523">  </div> <div data-bbox="486 523 813 794">  </div> <div data-bbox="409 801 880 858"> <p>I have 10 cubes, can you share them equally in 2 groups?</p> </div> <div data-bbox="486 858 813 1082">  </div>	<p>Children use pictures or shapes to share quantities.</p> <div data-bbox="927 427 1330 641"> <p>Sharing:</p>  <p>12 shared between 3 is 4</p> </div> <div data-bbox="927 721 1352 896">  <p>8 shared between 2 is 4</p> </div>	<p>12 shared between 3 is 4</p>	<div data-bbox="1921 156 2020 226">Y1</div> <div data-bbox="1975 529 2092 1050">Division</div>

Objective and Strategy	Concrete	Pictorial	Abstract	Y2
Division as sharing	<p>I have 10 cubes, can you share them equally in 2 groups</p> 	<p>Children use pictures or shapes to share quantities.</p>  <p>Children use bar modelling to show and support understanding.</p> <p>$12 \div 4 = 3$</p> 	<p>$12 \div 2 = 6$</p>	<h1>Division</h1>
Division as grouping	<p>Divide quantities into equal groups. Use cubes, counters, objects or PV counters to aid understanding.</p>  	<p>Use number lines for grouping.</p>  <p>$12 \div 3 = 4$</p> <p>Use the bar model, how many will go in each group?</p> 	<p>$28 \div 7 = 4$</p> <p>Use the inverse to help!</p>	
Division with remainders	See Year 3 for ideas as a GDS objective			

Objective and Strategy	Concrete	Pictorial	Abstract	Y3							
Division as grouping	<p>Use cubes, counters, objects or place value counters to aid understanding.</p> <p>24 divided into groups of 6 = 4</p>  <p>$96 \div 3 = 32$</p> 	<p>Continue to use bar modelling to aid solving division problems.</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p>	<p>How many groups of 6 in 24?</p> <p>$24 \div 6 = 4$</p>	Division							
Division with arrays	 <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>E.g. $15 \div 3 = 5$ $5 \times 3 = 15$</p> <p>$15 \div 5 = 3$ $3 \times 5 = 15$</p>	<p>Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p> 	<p>Find the inverse of multiplication and division sentences by creating eight linking number sentences.</p> <table><tr><td>$7 \times 4 = 28$</td><td>$4 \times 7 = 28$</td></tr><tr><td>$28 \div 7 = 4$</td><td>$28 \div 4 = 7$</td></tr><tr><td>$28 = 7 \times 4$</td><td>$28 = 4 \times 7$</td></tr><tr><td>$4 = 28 \div 7$</td><td>$7 = 28 \div 4$</td></tr></table>		$7 \times 4 = 28$	$4 \times 7 = 28$	$28 \div 7 = 4$	$28 \div 4 = 7$	$28 = 7 \times 4$	$28 = 4 \times 7$	$4 = 28 \div 7$
$7 \times 4 = 28$	$4 \times 7 = 28$										
$28 \div 7 = 4$	$28 \div 4 = 7$										
$28 = 7 \times 4$	$28 = 4 \times 7$										
$4 = 28 \div 7$	$7 = 28 \div 4$										

Objective and Strategy	Concrete	Pictorial	Abstract	Y3
Division with remainders.	<p> $14 \div 3 =$ Divide objects between groups and see how much is left over </p> 	<p> Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. </p>  <p> Draw dots and group them to divide an amount and clearly show a remainder. </p>  <p> Use bar models to show division with remainders. </p>  <p> Example without remainder: $40 \div 5$ Ask "How many 5s in 40?" </p>  <p> Example with remainder: $38 \div 6$ </p>  <p> For larger numbers, when it becomes inefficient to count in single multiples, bigger jumps can be recorded using known facts. </p>	<p> Complete the written divisions showing the remainders with an r. </p> <p> $29 \div 8 = 3 \text{ REMAINDER } 5$ </p> 	<h1>Division</h1>

Objective and Strategy	Concrete	Pictorial	Abstract	Y4-6
<p>Divide at least 3 digit numbers by 1 digit.</p> <p>Short Division</p>	<p>$96 \div 3$</p> <p>Use PV counters using the formal method alongside.</p> <div style="text-align: center;"> <div>T O</div> <div>3 2</div>  </div> <p>$42 \div 3 =$</p> <p>Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.</p> <div style="text-align: center;">  </div> <p>We exchange this ten for ten ones and then share the ones equally among the groups.</p> <div style="text-align: center;">  </div> <p>We look how much in 1 group so the answer is 14.</p>	<p>Continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.</p>  <p>Encourage them to move towards counting in multiples to divide more efficiently.</p>	<p>Begin with divisions that divide equally with no remainder. Encourage children to create a multiples line of the divisor.</p> <p>e.g. $872 \div 4$</p> <p>4 8 12 16 20 etc</p> <div style="text-align: center;">  </div> <p>Move to division with a remainder.</p> <div style="text-align: center;">  </div> <p>Introduce concept that the remainder can be expressed as a fraction.</p> <p>$432 \div 5 = 86 \frac{2}{5}$, with the remainder being the numerator and the denominator being the divisor.</p> <p>Finally move into decimal places to divide the total accurately.</p>	<h1>Division</h1>

			<div><div><div>14.6</div><div>1621</div></div><div>35</div><div>511.0</div></div>	
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Long division

Make sure the terminology – divisor, multiple, remainder, carry.

Step 1

Create a multiples line either using repeated addition or partitioning.

Repeated addition

$$\begin{array}{r}
 24 \\
 + 24 \\
 \hline
 48 \\
 + 24 \\
 \hline
 72 \\
 + 24 \\
 \hline
 96 \\
 + 24 \\
 \hline
 120
 \end{array}$$

1	0	+	4	=	4
2	0	+	8	=	8
3	0	+	12	=	12
4	0	+	16	=	16
5	0	+	20	=	20
6	0	+	24	=	24
7	0	+	28	=	28
8	0	+	32	=	32
9	0	+	36	=	36

See link for video:

<https://thirdspacelearning.com/blog/best-long-division-method-ks2/>

Step 2

Adopt the 'I, we, you' process to go through a worked example.

		543
1 - 24	24	$\overline{)13032}$
2 - 48		$\underline{-120}$
3 - 72		103
4 - 96		$\underline{-96}$
5 - 120		72
6 - 144		$\underline{-72}$
7 - 168		00
8 - 192		
9 - 216		

As working through make sure they understand the steps and encourage them to write the symbols for each step to secure the process.



Success criteria

1. List multiples of the divisor (are you going to do repeated addition or partition and add?)
2. Divide
3. Multiply
4. Subtract
5. Bring it down...
6. ...and bring it on back!

Step 3

Lots of practice and modelling.